

MC 0241 •  
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ATOMIC CONSTANTS, 1955 ADJUSTED VALUES, COMPUTED BY  
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TABLE OF CONSTANTS

Computed by W. B. Nottingham and based on the 1955 adjusted values of Atomic Constants  
in Tables 19 and 20, Handbuch der Physik, Vol. XXXV Atoms 1, 1957

	<u>m. k. s.</u>	<u>c. g. s.</u>
Avogadro's number $N_0$	$6.0249 \times 10^{26}$ molecules/kilo-mole	$6.0249 \times 10^{23}$ molecules/gram-mole
mass of a unit-atomic weight $1/N_0$	$1.6598 \times 10^{-27}$ kg	$1.6598 \times 10^{-24}$ gm
Loschmidt's constant $L_0 = N_0/V_0$	$2.6872 \times 10^{25}$ molecules/cu. m	$2.6872 \times 10^{19}$ molecules/cu cm
Boltzmann's constant (k)	$1.3804 \times 10^{-23}$ joule/degree	$1.3804 \times 10^{-16}$ erg/degree
gas constant $R = N_0 k$	$8.3170 \times 10^3$ joule/kilo-mole-degree	$8.3170 \times 10^7$ erg/gm-mole-degree
————— (calories)	$1.9878 \times 10^3$ cal/kilo-mole-degree	$1.9878 \times$ cal/gm-mole-degree
electron charge (e)	$1.6021 \times 10^{-19}$ coulomb	$4.8029 \times 10^{-10}$ statcoulomb
electron mass (m)	$9.1083 \times 10^{-31}$ kg	$9.1083 \times 10^{-28}$ gm
electron charge-mass ratio (e/m)	$1.7589 \times 10^{11}$ coulomb/kg	$5.2731 \times 10^{17}$ statcoulomb/gm
proton mass ( $M_P$ )	$1.67239 \times 10^{-27}$ kg	$1.67239 \times 10^{-24}$ gm
ratio (unit atomic wt.)/(electron wt.) ( $1/N_0 m$ )	1822.3	1822.3
Planck's constant (h)	$6.6252 \times 10^{-34}$ joule-sec	$6.6252 \times 10^{-27}$ erg-sec
————— cubed ( $h^3$ )	$2.9080 \times 10^{-100}$ (joule-sec) <sup>3</sup>	$2.9080 \times 10^{-79}$ (erg-sec) <sup>3</sup>
————— ( $h/2\pi$ )	$1.0544 \times 10^{-34}$ joule-sec	$1.0544 \times 10^{-27}$ erg-sec
velocity of light (c)	$2.99793 \times 10^8$ meter/sec	$2.99793 \times 10^{10}$ cm/sec
————— square ( $c^2$ )	$8.98758 \times 10^{16}$ meter <sup>2</sup> /sec <sup>2</sup>	$8.98758 \times 10^{20}$ cm <sup>2</sup> /sec <sup>2</sup>
mass of mercury atom	$3.330 \times 10^{-25}$ kg	$3.330 \times 10^{-22}$ gm
Faraday Constant $F = N_0 e$	$9.6522 \times 10^7$ coul/kilo-mole	$2.8937 \times 10^{14}$ statcoulomb/gm-mole

TABLE OF CONSTANTS (contd.)

	<u>m. k. s.</u>	<u>c. g. s.</u>
$\epsilon_0 = 10 / 4\pi c^2$	$8.8543 \times 10^{-12}$ farad/m	-----
$\mu_0 = 4\pi \cdot 10^{-7}$	$1.2566 \times 10^{-6}$ henry/m	-----
$4\pi \epsilon_0 = 10^7 / c^2$	$1.1127 \times 10^{-10}$ farad/m	-----
$(4\pi \epsilon_0)^{-1} = c^2 / 10^7$	$8.9874 \times 10^9$ meter/farad	-----
electron-volt equivalent of 1 cent. deg. (k/e)	$8.6164 \times 10^{-5}$ ev/degree	-----
temperature equivalent of 1 ev (e/k)	11,606 coulomb-degree/joule	-----
0.4343 e/k	5040 coulomb-degree/joule	-----
calorie per gm-mole equivalent of 1 ev ( $e N_0 / 4.1840$ )	-----	23,069 cal/gm-mole
kilo-cal per kg-mole equivalent of 1 ev ( $e N_0 / 4.1840$ )	23,069 kilo-cal/kg-mole	-----
frequency equivalent of 1.0 ev; (e/h)	$2.4182 \times 10^{14}$ cycles/sec	-----
wavelength equivalent of 1.0 ev; (hc/e)	$1.2397 \times 10^{-6}$ m	12,397 Å
density of Hg (at 20°C)	$13.546 \times 10^3$ kg/m. <sup>3</sup>	13.546 gm/cm <sup>3</sup>
acceleration of gravity (Cambridge, Mass.)	9.80398 meter/sec <sup>2</sup>	980.398 cm/sec <sup>2</sup>
ice point	273.16°K	273.16°K
volume of 1 gram-mole of a perfect gas; $V_0$ 1 std. atmo 0°C	-----	22.421 liters
volume of 1 kg-mole of a perfect gas; $V_0$ 1 std. atmo 0°C	22.421 cu. m	-----

### CONVERSION FACTORS

	<u>m.k.s.</u>	<u>c.g.s.</u>
1 standard atmosphere (76 cm Hg)	$1.0132 \times 10^5$ newton/m <sup>2</sup>	$1.0132 \times 10^6$ dyne/cm <sup>2</sup>
1 mm Hg pressure or 1 Tor	133.32 newton/m <sup>2</sup>	1333.2 dyne/cm <sup>2</sup>
1 Bar (approximately 1 atmosphere)	$10^5$ newton/m <sup>2</sup>	$10^6$ dyne/cm <sup>2</sup>
1 Barye ( $10^{-6}$ Bar)	$10^{-1}$ newton/m <sup>2</sup>	1 dyne/cm <sup>2</sup>
1 Angstrom unit	$10^{-10}$ m	$10^{-8}$ cm
1 micron	$10^{-6}$ m	$10^{-4}$ cm $10^{-3}$ mm
1 calorie	4.1840 joules	$4.1840 \times 10^7$ ergs
force (newton)	1 newton	$10^5$ dynes
current (ampere)	1 ampere (coulomb/sec)	$3 \times 10^9$ statcoulombs/sec
electric potential (volt)	1 volt	1/300 statvolts
mass of a unit atomic weight 1/N <sub>O</sub>	$1.6598 \times 10^{-27}$ kg	$1.6598 \times 10^{-24}$ gm

### SELECTED ATOMIC WEIGHTS

Electron  $5.487 \times 10^{-4}$

A = 39.9	Ne = 20.18	He = 4.033	O <sub>2</sub> = 32.0
H <sub>2</sub> = 2.016	N <sub>2</sub> = 28.02	Hg = 200.6	W = 184.0

### MATHEMATICAL CONSTANTS

base of natural logs(e) = 2.71821818	$1/\pi = 0.3183099$
$e^{-1} = 0.36788$	$4\pi = 12.5663706$
$(1 - e^{-1}) = 0.63212$	$1/4\pi = 0.0795775$
$\log_{10} e = 0.434294$	$\log_{10} \pi = 0.49715$
$\log_e 10 = 2.302585$	$\log_{10} 4\pi = 1.09921$
$\pi = 3.14159265$	$\log_e \pi = 1.14473$

### SOME USEFUL EQUATIONS

$$e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} \dots$$

$$\ln(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} \dots$$

$$\int_{-\infty}^{+\infty} e^{-a^2 x^2} dx = \frac{\sqrt{\pi}}{a}$$

$$\int_0^{\infty} x^n e^{-a^2 x^2} dx =$$

For even values of n:

$$n = 0 \dots \dots \dots = \frac{\sqrt{\pi}}{2a}$$

$$n = 2 \dots \dots \dots = \frac{\sqrt{\pi}}{4a^3}$$

$$n = 4 \dots \dots \dots = \frac{3\sqrt{\pi}}{8a^5}$$

$$\int_0^{\infty} x^n e^{-a^2 x^2} dx =$$

For odd values of n:

$$n = 1 \dots \dots \dots = \frac{1}{2a^2}$$

$$n = 3 \dots \dots \dots = \frac{1}{2a^4}$$

$$n = 5 \dots \dots \dots = \frac{1}{a^6}$$

## SOME USEFUL EQUATIONS (contd.)

Equation for particle current of Maxwell-Boltzmann gas:  $I = \frac{N}{V} \left( \frac{kT}{2\pi m} \right)^{1/2} = \frac{P}{(2\pi mkT)^{1/2}}$

For electrons at 300°K:  $\left( \frac{kT}{2\pi m} \right)^{1/2} = 2.690 \times 10^4$  m/sec;  $\frac{1}{(2\pi mkT)^{1/2}} = 6.4957 \times 10^{24}$

Equation of state for ideal gas:  $P = \frac{N}{V} kT$  = pressure;  $\frac{N}{V}$  = concentration of atoms (number/unit volume).

For potential energy  $\epsilon_c$  the constant  $\frac{a}{H^3} = \frac{N}{(2\pi mkT)^{3/2}} \left[ \iiint_V e^{-\frac{\epsilon_c}{kT}} dx dy dz \right]^{-1}$

For potential energy  $\epsilon_c = 0$ ;  $\frac{a}{H^3} = \frac{N}{V} (2\pi mkT)^{-3/2}$

$E$  = total kinetic energy per particle;  $f(E)$  = fraction of particles per unit range in energy with energy  $E$ .

Maxwell-Boltzmann energy distribution;  $f(E) dE = \frac{2\pi}{(\pi kT)^{3/2}} E^{1/2} e^{-\frac{E}{kT}} dE$ .

Fermi-Dirac energy distribution with  $n = (N/V)$ ;  $f(E) dE = \frac{8\sqrt{2} \pi m^{3/2}}{n h^3} \frac{E^{1/2} dE}{(e^{\frac{E - W_i}{kT}} + 1)}$

SOME USEFUL EQUATIONS (contd.)

Particle current  $I(W_x)$  in x-direction per unit energy range of  $W_x$  (Fermi statistics)

$$I(W_x) dW_x = \frac{4\pi mkT}{h^3} \ln \left( 1 + e^{-\frac{(W_x - W_i)}{kT}} \right) dW_x$$

For high concentrations of electrons:  $W_i = \frac{h^2}{2m} \left( \frac{3n}{8\pi} \right)^{2/3} \left\{ 1 - \frac{\pi^2}{12} \left[ \frac{kT}{\frac{h^2}{2m} \left( \frac{3n}{8\pi} \right)^{2/3}} \right]^2 + \right\}$

For  $T = 0$ ,  $W_i = \frac{h^2}{2m} \left( \frac{3n}{8\pi} \right)^{2/3}$

For low concentrations of electrons;  $W_i = -kT \ln \left[ \frac{2}{nh^3} (2\pi mkT)^{3/2} \right]$